

## Systematic dependence of asymmetric parameter in light and medium mass region

Reetu Kaushik<sup>1</sup> and S. Sharma<sup>\*</sup>

<sup>1</sup>Research Scholar, Department of Physics, Mewar University, Gangrar, Rajasthan-312901, India  
Panchwati Institute of Engineering and Technology (Uttar Pradesh Technical University),  
National Highway- 58, Ghat Institutional Area, Meerut, PIN 250005, INDIA

\*email: ss110096@gmail.com

### Introduction

The study of collective nuclear structure with  $N$ ,  $Z$ ,  $N_B$  and  $N_p N_n$  provide a detailed information of nuclear interactions involved. Several studies have been carried out to study the collectivity, deformation and systematic dependence of other nuclear properties on  $N_p N_n$ . de-Shalit & Goldhaber [1] pointed out the important role of valence nucleons. Talmi [2] noted the constancy of nuclear level structure in semi-magic isotones/isotopes. Hamamoto [3] observed that the  $p^+$  &  $n^0$  both are required for producing deformation. In IBM-1[4], the structure of nuclei depends on the total boson numbers  $N_B$ . The concept of F-spin multiplets was based on this and was well explained by Brentano et al. [5]. Casten [6] noted that the  $E_{2g^+}$  have smooth dependence on  $N_p N_n$ . Various studies [7] have been carried out to study the collectivity, deformation and systematic dependence of various nuclear observables on the product  $N_p N_n$ .

Gupta [8] observed that  $1/\alpha$  was linearly dependent on  $N_p N_n$ , where the coefficient  $\alpha$  contributes for rotational part of energy in the SU(3) symmetry limit of IBM[4] as,

$$E([N](\lambda, \mu) \text{ KLM}) = \alpha L(L+1) + \beta C(\lambda, \mu)$$

The  $B(E2; 2_1^+ \rightarrow 0_1^+)$  values were also related with  $N_p N_n$ . Gupta et al. [9] noted a systematic dependence of  $\gamma$ -g  $B(E2)$  ratios on the  $N_p N_n$  in different parts of the major shell space  $Z=50-82$ ,  $N < 82$  and  $N=82-126$ . Casten and Zamfir [6] presented a review on the evolution of nuclear structure based on  $N_p N_n$  product. The  $N_p N_n$  scheme was further modified to use P- factor [9].

In this paper, we study the role of valence nucleons and holes on the nuclear structure, through  $N_p N_n$ . Casten and Zamfir [7] covered the various regions, viz.,  $A=100, 130, 150$  ( $Z < 64$ ,  $Z > 64$ ) and  $A=190$ . We present our results for  $50 \leq Z \leq 82$  and  $82 \leq N \leq 126$  region on *quadrant wise basis*.

The values of asymmetry parameter ( $\gamma$ ) have been calculated for  $50 \leq Z \leq 82$  and  $82 \leq N \leq 126$  region and the whole data is divided into four quadrants and it has been plotted with  $N_p N_n$  to study its systematics dependence.

### Calculation of Asymmetric Parameter

The value of  $\gamma$  can be evaluated using the experimental energies  $E_{2_2^+}$  and  $E_{2_1^+}$  states [10]. The energy ratio  $R\gamma = E_{2_2^+} / E_{2_1^+}$  and  $\gamma$  is:

$$\gamma = (1/3) \sin^{-1} [(9/8) \{1 - ((R\gamma - 1)/(R\gamma + 1))^2\}]$$

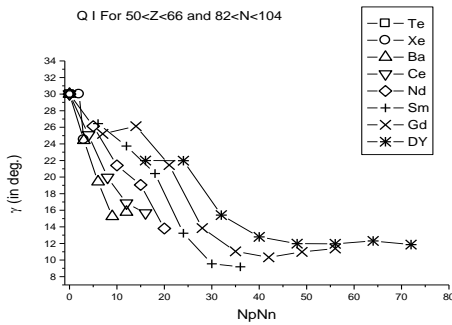
It can be evaluated using: (a) The energy ratio  $R_4 = (E_{4g}/E_{2g})$  but only the nuclei with  $2.8 \leq R_4 \leq 3.33$  will be allowed [11, 12]. (b) The  $B(E2)$  values which are very small and available with uncertainties. Therefore the values from energy ratio  $R\gamma$  are more reliable.

### Result and discussions

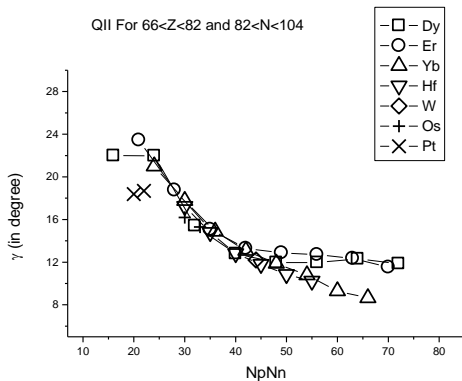
The variation of  $\gamma$  versus  $N_p N_n$  product for quadrant-I for  $50 \leq Z \leq 66$  and  $82 \leq N \leq 104$  has been shown in Fig. 1. There is smooth dependence of  $\gamma$  with  $N_p N_n$ . The  $\gamma$  decreases from a maximum value of  $30^\circ$  for  $N_p N_n = 0$  (i.e. SU(5) limit of IBM) to a minimum values of about  $9^\circ$  (i.e. SU(3) limit of IBM). The  $\gamma$  saturates for  $N_p N_n \geq 30$ . This shows non-dependence of  $\gamma$  with  $N_p N_n$

because for a fixed value of  $N_p N_n$  the  $\gamma$  is having varying values.

The variation of  $\gamma$  versus  $N_p N_n$  for quadrant-II for  $66 \leq Z \leq 82$  and  $82 \leq N \leq 104$  has been shown in Fig. 2. There is smooth dependence of  $\gamma$  with  $N_p N_n$  except Yb for  $N_p N_n > 50$  and few Pt isotopes.



**Fig.1** The variation of asymmetric parameter ( $\gamma$ ) versus  $N_p N_n$ .



**Fig. 2** The variation of asymmetric parameter ( $\gamma$ ) versus  $N_p N_n$  product for quadrant-II.

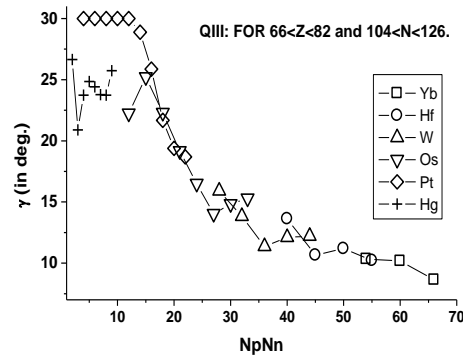
The variation of  $\gamma$  versus  $N_p N_n$  for quadrant-III for  $66 \leq Z \leq 82$  and  $104 \leq N \leq 126$  has been shown in Fig. 3. There is smooth dependence of  $\gamma$  with  $N_p N_n$  except Hg isotopes.

The graphs of  $\gamma$  against  $N_p N_n$  vividly displays the formation of isotonic multiplets in quadrant-I, strong dependence on  $N_p N_n$  in quadrant-II and weak constancy with  $Z$  in

quadrant-III is illustrated and support the findings of Gupta [13].

### Acknowledgements

We are grateful to Professor J. B. Gupta for his valuable guidance. SS express his gratitude Shri Pankaj Goel, Chairman, PIET, Meerut for providing the facilities for the research work



**Fig. 3** The variation of asymmetric parameter ( $\gamma$ ) versus  $N_p N_n$  product for quadrant-III.

### References

- [1] A. deShalit and M. Goldhaber, Phys. Rev. **92**, 1211(1953).
- [2] I. Talmi, Rev. Mod. Phys. **34**, 704 (1953).
- [3] I. Hamamoto, Nucl. Phys. **73**, 225 (1965).
- [4] R.F. Casten, *Nuclear Structure from a Simple Perspective* (IInd Edition, Oxford University Press, 2001).
- [5] P. von Brentano et. al., J. Phys. *G11*, L85 (1985).
- [6] R. F. Casten, Nucl. Phys. **A443**, 1 (1985).
- [7] R. F. Casten and N.V. Zamfir, J. Phys. *G Nucl. Part. Phys.* **22**, 1521(1996).
- [8] J. B. Gupta, Phys. Rev. *C33*, 1505 (1986).
- [9] J. B. Gupta, J.H. Hamilton and A.V. Ramayya, Phys. Rev. **C42**, 1373 (1990).
- [10] Recent data for energies have been taken from <http://www.nndc.bnl.gov>
- [11] S. Sharma, Ph. D. Thesis, University of Delhi (1989) unpublished.
- [12] J. B. Gupta and S. Sharma, Physics Scripta, **39**(1989)50.
- [13] J. B. Gupta, Eur. Phys. J. A. **48**(2012)177.